

November 25, 2017

2:30-5:30

## END-Semester Examination ME-601: CAGD

Duration: 180 Min. Maximum Marks: 100 All questions are compulsory.

- 1. Write a procedure to truncate a parametric cubic curve segment at two specified values of u and subsequently reparametrize it. Test your formulation for a parametric cubic curve with a given set of end points  $P_0(1,1,1)$  and  $P_1(4,2,4)$  and the end tangents  $p^u(0)=(1,1,0)$  and  $p^u(1)=(1,1,1)$  truncated at :
  - a. u = 0.25 and u = 0.75,
    b. u = 0.333 and u = 0.667 (15)
- 2. Show that a fourth order B Spline curve with four defining polygon vertices using open uniform knot vector yields a cubic Bezier curve. (15)
- 3. Write down the parametric equation of following.
  - a. A straight line joining points (1, 1, 1) and (10, 2, 3)
  - b. A semi circular arc of radius 6 units lying in y = 20 plane. The arc has starting point at (13, 20, 0) lies completely above x-axis with center at (7, 20, 0).
  - c. Write down the parametric equation of ruled surface defined by joining above two curves.
  - d. Find out coordinates of point (u = 0.5, w = 0.5) on the above surface. (15)
- 4. What is an average and Gaussian curvature with respect a parametric surface. Explain, How to decide whether given surface is developbale or not. (15)
- 5. Define a Bezier curve with four polygon vertices  $B_1[1\ 1]$ ,  $B_2[2\ 3]$ ,  $B_3[4\ 3]$  and  $B_4[3\ 1]$ , split this curve into two curves each one being a cubic Bezier curve and find out the control points of these two curves if the original curve is split at point corresponding to parametric value u=0.5. (20)
- 6. Briefly explain following terms and phrases.

(4x5)

- a. Regularized Boolean Operation
- b. Explain Conditions for C<sup>0</sup> and C<sup>1</sup> continuity between two Bezier patches along a common boundary.
- c. Explain use and need of the homogeneous coordinates
- d. Explain the advantage of Representing curves and surfaces as NURBS